

受験番号 _____

氏名 _____

問 1

$$\begin{aligned}
 1) \quad & x^3 - x^2y - xz^2 + yz^2 \\
 & = x^2(x - y) - z^2(x - y) \\
 & = (x^2 - z^2)(x - y) \\
 & = (x + z)(x - z)(x - y)
 \end{aligned}$$

$$\begin{aligned}
 2) \quad & 2x^2 + 6y^2 - z^2 + 7xy - yz - xz & 1 \quad & 2y - z \\
 & = 2x^2 + 7xy - xz + 6y^2 - yz - z^2 & 2 \quad & 3y + z \\
 & = 2x^2 + (7y - z)x + (2y - z)(3y + z) \\
 & = (x + 2y - z)(2x + 3y + z)
 \end{aligned}$$

問 2

$$\begin{aligned}
 1) \quad & 2x^2 + 5x = 3 \\
 & (x + 3)(2x - 1) = 0 \\
 & \therefore x = \frac{1}{2}, -3
 \end{aligned}$$

$$\begin{aligned}
 2) \quad & 2x + 1 < x - 3 \leq 3x + 7 & x < -4 \\
 & 2x + 1 < x - 3 & -2x \leq 10 \\
 & & x \geq -5
 \end{aligned}$$

$$\therefore -5 \leq x < -4$$

$$\begin{aligned}
 3) \quad & x^2 + 2x - 3 < 0 \\
 & (x + 3)(x - 1) < 0
 \end{aligned}$$

$$\therefore -3 < x < 1$$

$$4) \quad |x + 1| + |x - 3| > 4x + 3$$

i) $x < -1$ のとき

$$-(x + 1) - (x - 3) > 4x + 3$$

$$-2x + 2 > 4x + 3$$

$$-6x > 1$$

$$x < -\frac{1}{6}$$

よって $x < -1$ iii) $x \geq 3$ のとき

$$x + 1 + x - 3 > 4x + 3$$

$$2x - 2 > 4x + 3$$

$$-2x > 5$$

$$x < -\frac{5}{2}$$

不適切

ii) $-1 \leq x < 3$ のとき

$$x + 1 - (x - 3) > 4x + 3$$

$$-4x > 3 - 4$$

$$x < \frac{1}{4}$$

よって $-1 \leq x < \frac{1}{4}$

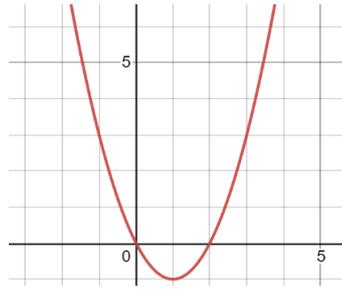
$$\therefore x < \frac{1}{4}$$

問 3

1) $y = a(x - 2) \cdot x$ とおく
点(3・3)を通るので
 $3 = a(3 - 2) \cdot 3$
 $a = 1$
 $\therefore y = x(x - 2)$

2) $y = x^2 - 2x$
 $y = (x - 1)^2 - 1$

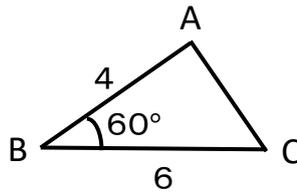
最小値 $x = 1$ のとき -1
最大値 $x = -2$ のとき 8



問 4

1) $S = \frac{1}{2} \times 4 \times 6 \times \sin 60^\circ$
 $= 6\sqrt{3}$

A. $6\sqrt{3} \text{ cm}^2$



2) $AC^2 = 4^2 + 6^2 - 2 \cdot 4 \cdot 6 \cdot \frac{1}{2}$
 $= 16 + 36 - 24$
 $= 28$

$AC > 0$ より

$AC = 2\sqrt{7}$

$\therefore 2\sqrt{7} \text{ cm}$

3) $\frac{AC}{\sin 60^\circ} = \frac{2\sqrt{7}}{\frac{\sqrt{3}}{2}} = \frac{4\sqrt{7}}{\sqrt{3}} = \frac{4}{3}\sqrt{21}$

$= \frac{4}{3}\sqrt{21} \text{ cm}$